

Introduction

- Zero-net mass flux (ZNMF) actuated incompressible turbulent jets can be studied effectively with DNS simulations at a moderate Reynolds number ($Re=2000$).
- DNS with OpenFOAM requires excessive number of grid elements because of second order accuracy.
- Two main problems for high fidelity simulations in OpenFOAM:
 - High time step cost because of solving Pressure-Poisson equation multiple times in pisoFoam:

→ **projectionFoam**
 - Limited HPC capabilities due to inefficient scaling:

→ **parallel statistical averaging**

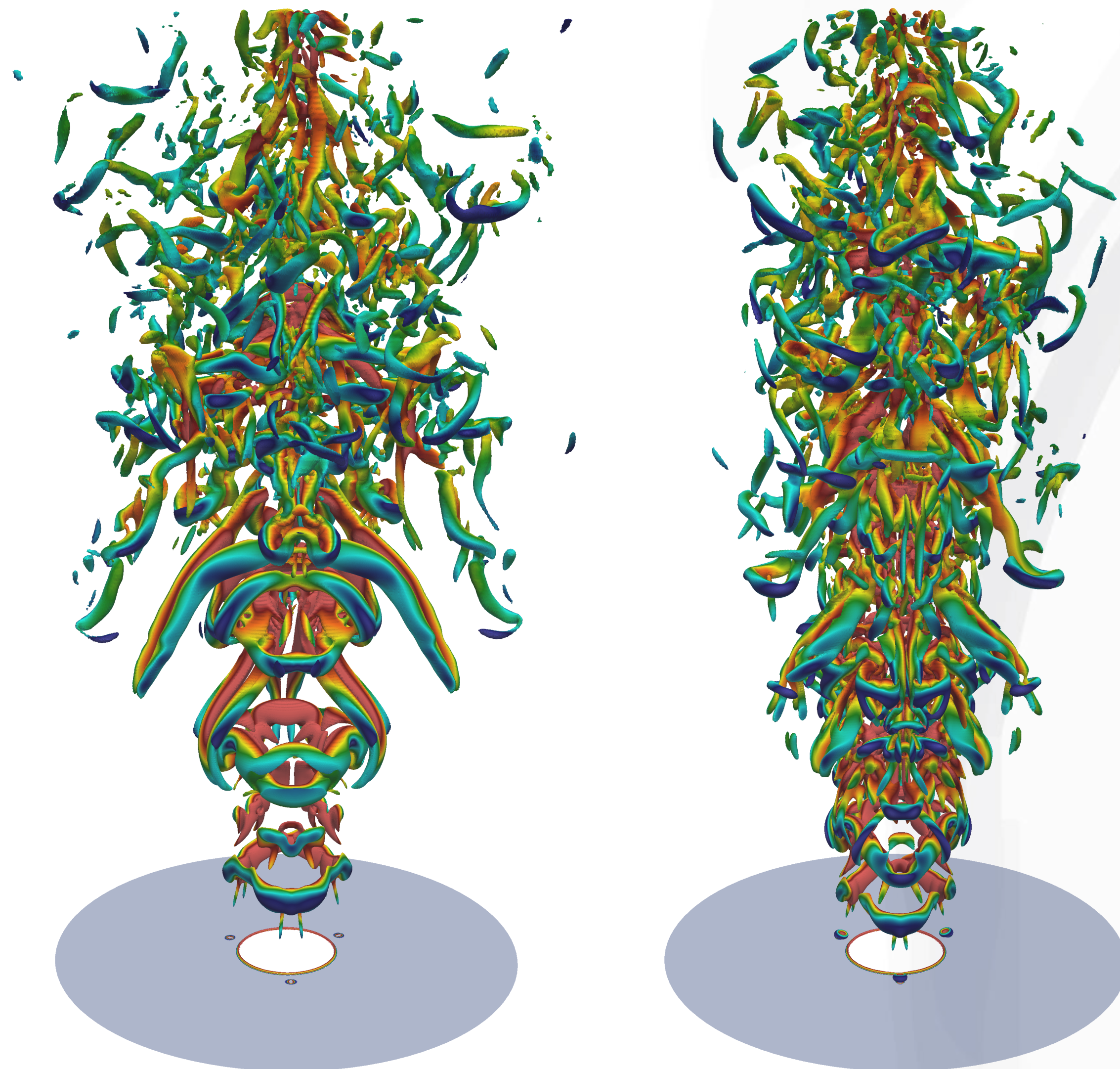


Figure 1: Vortex structures in ZNMF actuated round jets using Q criterion. Actuated with (left): preferred mode frequency; (right): first subharmonic of preferred mode frequency.

Methods

- A new transient solver entitled "**projectionFoam**" is implemented to replace iterative pisoFoam and reduce the time step cost.
- projectionFoam is based on incremental projection scheme¹ which keeps the second order temporal accuracy for velocity.
- Second order extrapolation is employed for convective flux to ensure second order overall accuracy in time.

projectionFoam

- Second order extrapolation for convective flux:


```
phi_o=0.5*(3.0*phi.oldTime()-phi.oldTime().oldTime());
```
- Momentum step:


```
fvVectorMatrix UEqn ( fvm::ddt(U)
+ fvm::div(phi_o, U) + turbulence->divDevReff(U));
solve(UEqn == -fvc::grad(p));
```
- Modification for Rhie-Chow interpolation:


```
U += dt*fvc::grad(p);
```
- Projection step:


```
fvScalarMatrix pEqn(fvm::laplacian(dt, p) ==fvc::div(phi));
pEqn.solve();
U -= dt*fvc::grad(p);
```

* Full source code is submitted to Unsupported Contributions Repository of the OpenFOAM foundation. Additionally it is available on Ref. 2.

- Parallel scalability performance was found insufficient to do a DNS simulation in a feasible time margin. To overcome this problem we employed **parallel statistical averaging**^{3,4}. It is a hybrid concept to calculate statistical moments combining time averaging with ensemble averaging:

$$\langle u(x) \rangle \approx \frac{1}{R} \sum_{r=1}^R \frac{R}{T_s} \int_{t_0}^{t_0+T_s/R} u^{\{r\}}(x, t) dt$$

- We start R turbulent flow simulations with different initial disturbances to allow statistical independency among them. Once the turbulence is fully developed, we collect statistics in every member of the ensemble.
- Parallel statistical averaging allows additional speed-up by reducing the statistics collection time T_s to T_s/R .

Results

Validation of projectionFoam

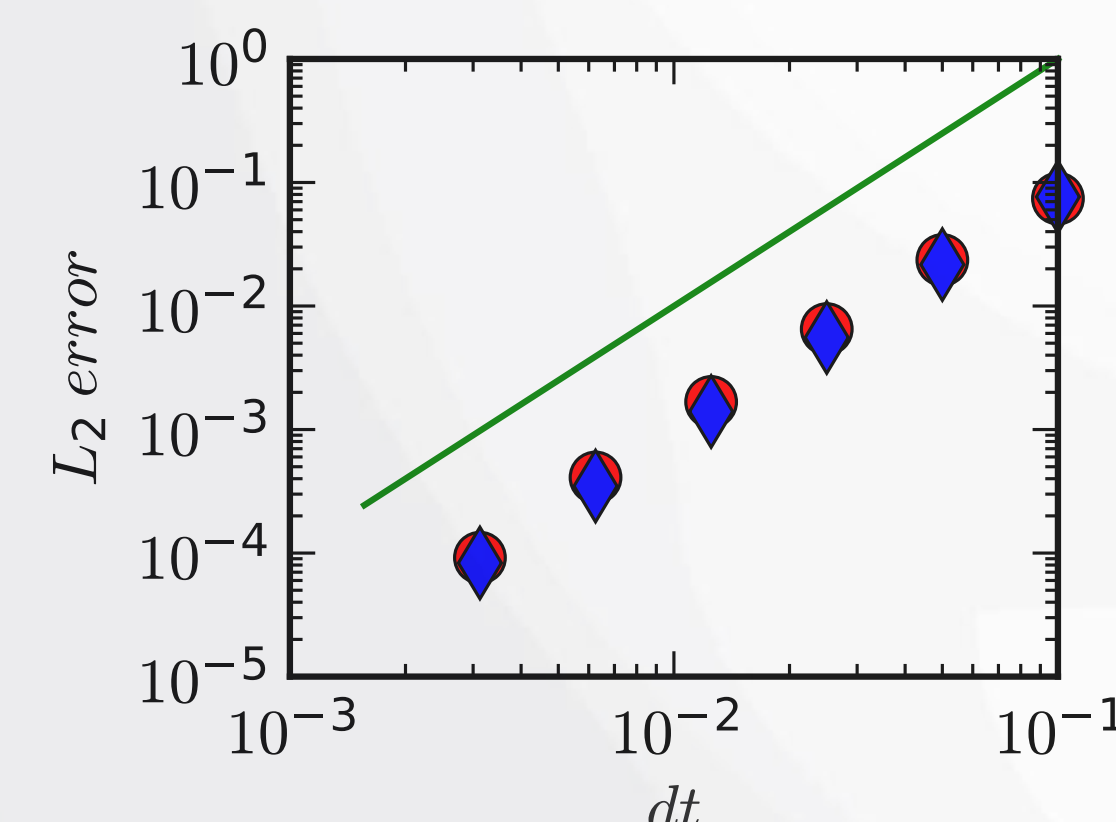


Figure 2: Error for Taylor-Green vortex case using Crank-Nicolson time integration. (•): pisoFoam; (♦): projectionFoam; (—): slope=2

DNS of a controlled jet with 124.117.500 elements

- Parallel performance test on Tier-1 supercomputer of Flemish Supercomputer Center equipped with Intel Sandy Bridge microprocessors and FDR Infiniband Mellanox communication network:

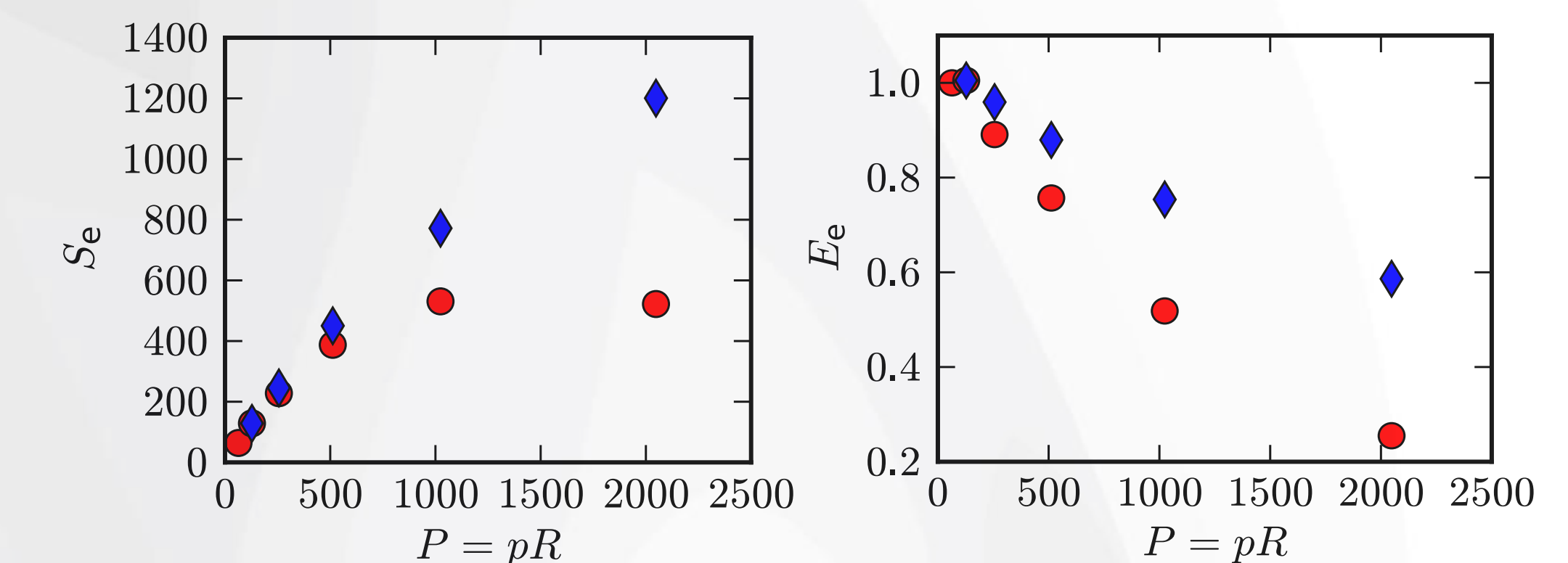


Figure 3: (left): speed-up; (right): parallel efficiency. (•): only domain decomposition; (♦): domain decomposition combined with parallel statistical averaging.

- $P=624$ processors ($p=156$, $R=4$) are employed and speed-up of $S_e=540.56$ and parallel efficiency of $E_e=0.87$ are obtained.
- Solver performance on 128 processors:

	execution time	# Poisson solutions
pisoFoam	71.5 s	2
projectionFoam	49.1 s	1

Summary and Conclusion

- projectionFoam allowed a performance gain above 30% over pisoFoam.
- Speed-up and efficiency can be effectively increased by using parallel statistical averaging in combination with domain decomposition parallelism.

References

- J. van Kan. A second-order accurate pressure correction scheme for viscous incompressible flow. SIAM J. Sci. Stat. Comput., 7(3):870–891, July 1986.
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- D. Carati, M. Rogers, and A. Wray. Statistical ensemble of large-eddy simulations. Journal of Fluid Mechanics, 455:195–212, MAR 25 2002
- A. Onder, P. Wu, and J. Meyers. Improving speed-up and efficiency in simulation of stationary turbulent flows by parallelization of statistical averaging. In Proceedings of the 9th International ERCOFTAC Symposium on Engineering Turbulence Modeling and Measurements (ETMM9), June 2012.

Acknowledgements

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